BGE S1-S3 Mathematics & Numeracy



Second Level

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Introduction to BGE Mathematics

How to get the most from this book

Mathematics is the richest language in the world. Learning mathematics is one of the most important things you can do to boost your brain power, now and throughout your life. Mathematicians understand, describe and influence the world around us. This book covers all the BGE Benchmarks for Mathematics at Second Level.

The chapters take you on a journey which will both support and challenge you. As you focus and work hard on each section you will gain knowledge, understanding and the ability to solve problems and communicate your solutions to others.

Working through this book will equip you to be the best mathematician you can be. Every topic is explained with rigour, taking no short cuts, and has an abundance of practice and challenge to suit every learner. The book is ambitious, encouraging you to aim high and build the skills you need for future success.

The book is enjoyable and easy to read. Every topic includes a clear, 'straight-to-the-point' method set out using bullet points in concise and simple language. It is full of worked examples and helpful hints and contains proven methods for mastering difficult concepts. This book has been designed both as a classroom aid and for your personal study.



We hope that you enjoy using this book as much as we have enjoyed creating the content, questions and activities for you!

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test your skills

with the most challenging problems.

Multiplying whole numbers by a single digit

To multiply whole numbers by a single digit:

- Set out the calculation neatly as shown here.
- Multiply the digits in each place value in turn. Start from the units on the right.
- If the result is 10 or greater, set down the units digit and carry the tens digit into the next column. See the Worked examples below.

The **product** of two numbers is the result of multiplying them together.

| 1 Calculate: a) 21×4 b) 624×8 c) 8596×9 $\times \frac{2}{4} \frac{4}{8 - 4}$ $\times \frac{6}{4 - 9} \frac{2}{9 - 2}$ $\times \frac{8}{5} \frac{5}{9} \frac{9}{6}$ 2 A venue sells 4424 tickets each costing £7. Calculate the total takings. The total takings are £30 968. $\times \frac{2}{3} \frac{1}{0} \frac{2}{9} \frac{7}{6} \frac{7}{8}$ Look at example 1a). There is no need to carry any digits. Step 1 $4 \times 1 = 4$ Step 2 $4 \times 2 = 8$ Look at example 1b). You have to carry twice. Step 1 $8 \times 4 = 32$. Set down the 2 units and carry the 3 (tens) into the next column. Step 2 $8 \times 2 = 16$ and add the 3 (tens) you carried, $16 + 3 = 19$ (tens). You set down the 9 (tens) and carry the 1 (hundred) into the next column. Remember 10 tens is 100. Step 3 $8 \times 6 = 48$ and add the 1 you carried, $48 + 1 = 49$ (hundreds). As this is the last place value you set down both digits. Exercise 1E 1 Set down and multiply: a) $3 4$ b) $2 3$ c) $1 6$ d) $4 7$ $\times 2$ $\times 3$ $\times 4$ $\times 5$ $\times 4$ $\times 5$ e) $2 4 1 1$ f) $1 5 2$ g) $4 1 2$ h) 7 $8 4$ $\times 2$ $\times 3$ $\times 4$ $\times 6$ $\times 6$ $\times 6$ $\times 6$ | |
|--|--|
| a) 21×4 b) 624×8 c) 8596×9 $\times \frac{2}{4} \frac{4}{8 - 4}$ $\times \frac{6}{4 - 9} \frac{2}{9 - 2}$ $\times \frac{8}{5} \frac{5}{9} \frac{9}{6}$ $\times \frac{4}{8 - 4}$ $\times \frac{1}{4 - 9} \frac{3}{9 - 2}$ $\times \frac{8}{7 - 7} \frac{5}{3} \frac{8}{6 - 4}$ 2 A venue sells 4424 tickets each costing f.7. Calculate the total takings. $\times \frac{2}{3} \frac{1}{0 - 9} \frac{2}{6} \frac{7}{8}$ Look at example 1a). There is no need to carry any digits. Step 1 $4 \times 1 = 4$ Step 2 $4 \times 2 = 8$ Look at example 1b). You have to carry twice. Step 1 $8 \times 4 = 32$. Set down the 2 units and carry the 3 (tens) into the next column. Step 2 $8 \times 2 = 16$ and add the 3 (tens) you carried, $16 + 3 = 19$ (tens). You set down the 9 (tens) and carry the 1 (hundred) into the next column. Remember 10 tens is 100. Step 3 $8 \times 6 = 48$ and add the 1 you carried, $48 + 1 = 49$ (hundreds). As this is the last place value you set down both digits. Exercise 1E 1 Set down and multiply: a) $3 4$ b) $2 3$ c) $1 6$ d) $4 7$ $\times 2$ $\times 3$ $\times 4$ $\times 5$ $\times 4$ $\times 5$ e) $2 4 1 f$ $1 5 2$ g) $4 1 2$ h) 7 $8 4$ $\times 2$ $\times 3$ $\times 4$ $\times 6$ $\times 6$ $\times 6$ | 1 Calculate: |
| $\begin{array}{c} 2 & 1 \\ \times \frac{4}{8 + 4} \\ \times \frac{1}{4 + 9} \\ \frac{1}{9 + 9} \\ \frac{3}{2} \\ \end{array} \\ \begin{array}{c} x \\ x \\ \frac{4}{8 + 4} \\ \end{array} \\ \begin{array}{c} x \\ \frac{1}{4 + 9} \\ \frac{1}{9 + 9} \\ \frac{3}{2} \\ \end{array} \\ \begin{array}{c} x \\ x \\ \frac{1}{4 + 9} \\ \frac{3}{9 + 9} \\ \frac{3}{2} \\ \end{array} \\ \begin{array}{c} x \\ x \\ \frac{2}{1 + 2 + 7} \\ \frac{2}{3 + 0} \\ \frac{7}{7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{7 + 7 + 3} \\ \frac{5}{8 + 5 + 9} \\ \frac{5}{8 + 4} \\ \frac{1}{2 + 7} \\ \frac{7}{3 + 0} \\ \frac{7}{7 + 3} \\ \frac{7}{8 + 4} \\ \frac{7}{8 + 1} \\ \frac{7}{8 + 1}$ | a) 21 × 4 b) 624 × 8 c) 8596 × 9 |
| $\frac{4}{8} + \frac{7}{4} + \frac{1}{9} + \frac{3}{9} + \frac{3}{2} + \frac{3}{7} + \frac{3}{7} + \frac{3}{7} + \frac{3}{3} + \frac{3}{6} + \frac{3}{4} + \frac{3}{9} + \frac{3}{2} + \frac{3}{7} + \frac{3}{7} + \frac{3}{7} + \frac{3}{3} + \frac{3}{6} + \frac{3}{4} + \frac{3}{9} + \frac{3}{2} + \frac{3}{7} + \frac{3}{7} + \frac{3}{7} + \frac{3}{3} + \frac{3}{6} + \frac{3}{4} + \frac{3}{2} + \frac{3}$ | |
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| Exercise 1E 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 $\times 2^{2} \times 3^{3} \times 4^{2} \times 5^{5}$ e) 2 4 1 f) 1 5 2 g) 4 1 2 h) 7 8 4 $\times 2^{2} \times 3^{3} \times 4^{3} \times 6^{5}$ | |
| 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 $\times 2^{2} \times 3^{3} \times 4^{2} \times 5^{3}$ e) 2 4 1 f) 1 5 2 g) 4 1 2 h) 7 8 4 $\times 2^{2} \times 3^{3} \times 4^{3} \times 6^{3}$ | |
| a) $3 \ 4 \ b) \ 2 \ 3 \ c) \ 1 \ 6 \ d) \ 4 \ 7 \ x \ 2 \ c) \ 1 \ 6 \ d) \ 4 \ 7 \ x \ 5$ e) $2 \ 4 \ 1 \ f) \ 1 \ 5 \ 2 \ g) \ 4 \ 1 \ 2 \ h) \ 7 \ 8 \ 4 \ x \ 6 \ c)$ | Exercise 1E |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | Exercise 1E 1 Set down and multiply: |
| e) 2 4 1 f) 1 5 2 g) 4 1 2 h) 7 8 4 × 2 × 3 × 6 \rightarrow | Exercise 1E 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | Exercise 1E 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 $\times 2$ $\times 3$ $\times 4$ $\times 5$ |
| | Exercise 1E 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 $\times 2$ $\times 3$ $\times 4$ $\times 5$ c) 2 4 1 5 2 $\times 1$ $\times 4$ $\times 5$ |
| • | Exercise 1E 1 Set down and multiply: a) 3 4 b) 2 3 c) 1 6 d) 4 7 $\times 2$ $\times 3$ $\times 4$ $\times 5$ e) 2 4 1 f) 1 5 2 g) 4 1 2 h) 7 8 4 $\times 2$ $\times 4$ $\times 6$ |

Multiplying whole numbers by a single digit



5 Angles

Types of angles

Whenever two straight lines meet, an angle is formed. An angle is a measure of the turn between two straight lines. The units we use to measure angles are called degrees and the instrument we use is called a **protractor**. We use the symbol ° as a shorthand for degrees.



Types of angles

Worked examples

1 Choose the correct word to describe each marked angle in these diagrams.



a) 70°
b) 219°
c) 104°
104° is between 90° and 180°, so it is a reflex angle.
is an acute angle.
c) 104°
c) 104°<





m)

3



0)



Choose the correct word from the following list to describe each angle. acute, right, obtuse, straight, reflex, full turn

| a) | 40° | b) | 120° | c) | 100° | d) | 90° | e) | 250° |
|-----------|------|-----------|------|-----------|------|-----------|------|----|------|
| f) | 145° | g) | 75° | h) | 315° | i) | 205° | j) | 85° |
| k) | 107° | l) | 3° | m) | 219° | n) | 141° | o) | 180° |
| P) | 58° | q) | 1° | r) | 183° | s) | 136° | t) | 314° |
| u) | 155° | v) | 360° | w) | 91° | x) | 89° | y) | 280° |

6 Measurement

Reading scales

When reading scales, you may have to work out the value of each space first.





Quadrilaterals and polygons

A **quadrilateral** is a shape with 4 straight **edges** (or sides). The edges meet at a **vertex** (or corner). The plural of vertex is **vertices**. A straight line from one vertex to another vertex which is not an edge is called a **diagonal**.

More generally, any 2D shape with straight edges is a **polygon**. When all sides of a polygon are the same length, it is a **regular** polygon. When the sides are not the same length, the polygon is **irregular**.

| Worked examples Copy and complete the tables. | | | | | | | |
|---|-------------------------|----------|--|--|--|--|--|
| ¹ _ + | Name Number of edges | | The small lines tell you that each edge is the | | | | |
| | Number of vertices | | same length so the quadrilateral is a square. | | | | |
| I | Number of diagonals | | | | | | |
| | Name | Square | | | | | |
| | Number of edges | 4 | There are four edges (shown in blue). | | | | |
| | Number of vertices | 4 | There are four vertices (shown in green). | | | | |
| | Number of diagonals | 2 | There are two diagonals (shown in red). | | | | |
| 2 | Name | | A polygon with 5 edges is a pentagon. | | | | |
| \times | Regular? | | The small lines tell you that each edge is the | | | | |
| | Number of edges | | same length so the polygon is regular. | | | | |
| \uparrow \uparrow | Number of vertices | | | | | | |
| | Number of diagonals | | | | | | |
| | Name | Pentagon | | | | | |
| | Regular? | Yes | | | | | |
| | Number of edges | 5 | There are five edges (shown in blue). | | | | |
| | Number of vertices | 5 | There are five vertices (shown in green). | | | | |
| ¥¥ | Number of diagonals | 5 | There are five diagonals (shown in red). | | | | |

Other quadrilaterals and polygons include:



Exercise 7F

1 Copy and complete the table to show which of the following shapes are quadrilaterals and which are examples of other polygons. The first two have been done for you.

| Shape | Quadrilateral | Other Polygon | A | в | c c |
|-------|-----------------------|------------------|---|---|-----|
| А | ✓ | | | | |
| В | | 1 | | | |
| С | | | | | |
| D | | | D | E | E |
| E | | | | | r - |
| F | | | | | |
| G | | | | | |
| Н | | | G | Н | |
| | | | | | |

- 2 Name each of the shapes in Q1. Choose from kite, octagon, rhombus, hexagon, rectangle, pentagon, heptagon, parallelogram.
- **3** Copy and complete the following tables for the shapes given. Draw a sketch of the shape and mark the diagonals if this helps you.

| a) | Name | Ь) | \frown | Name | |
|-----|---------------------|----|--------------|---------------------|---|
| | Number of edges | | \backslash | Number of edges | |
| | Number of vertices | | \backslash | Number of vertices | |
| | Number of diagonals | | | Number of diagonals | |
| | Name | d) | | Name | |
| | Regular? | | | Regular? | |
| f f | Number of edges | | | Number of edges | |
| | Number of vertices | | | Number of vertices | |
| | Number of diagonals | | | Number of diagonals | , |
| | | | | | |

4 Each diagram below is produced by joining two shapes together. Write down the two shapes used in each diagram.



13 Data

Check-up

- 1 Bill is doing a survey to find out about sleep habits. He plans this question:
 - Q. Do you get lots of sleep?
 - a) Do you think Bill's question will produce good data? Explain your answer.
 - b) Write a better question for Bill. Include options for the answer.
- 2 Kaiwan carries out a traffic survey. He records the data shown here.

car, bike, van, car, car, bus, van, bike, car, van, bike, scooter, car, bike, car, car, bus, van, bike, car, scooter, bike, car, bus, bike, bus, car, bike, car, bike, van, car, scooter, bike

a) Copy and complete the frequency table to organise the data.

| Vehicle | Tally | Frequency |
|---------|-------|-----------|
| Car | | |
| Bus | | |

- b) List the vehicle types from most to least common.
- c) Find the total number of bikes and scooters.
- d) Find the total number of vans, buses and cars.
- 3 A leisure centre records data on customer visits one Sunday. The bar graph shows the results.
 - a) List the activities from most to least popular.
 - b) How many customers used the sauna?
 - c) The manager thinks swimming is three times more popular than rackets. Do you agree? Give evidence.
 - d) Find the difference between the number of customers using the gym and the number going for a swim.
 - e) All the visitors only did one activity. Calculate the total number of visitors that Sunday.



- 4 The table shows the number of goals scored at the 2018 FIFA World Cup by players from different leagues around the world.
 - a) Draw a bar chart to display the data.

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- b) List the leagues from the most goals scored to the least.
- c) How many more goals were scored by players from La Liga than by players from Serie A?
- d) Jen thinks the Premier League players scored four times as many goals as the Ligue 1 players. Is Jen correct? Give evidence for your answer.

| League | Number of goals scored |
|----------------|---------------------------|
| Bundesliga | 13 |
| Serie A | 8 |
| Ligue 1 | 14 |
| Premier League | 46 |
| La Liga | 36 |

- 5 The table shows the results of a test on a disposable coffee cup.
 - a) Draw a line graph to display the results.
 Set up your axes as shown.



| Disposable coffee cup | | | | | |
|-----------------------|------------------|--|--|--|--|
| Time (minutes) | Temperature (°C) | | | | |
| 0 | 60 | | | | |
| 10 | 40 | | | | |
| 20 | 35 | | | | |
| 30 | 25 | | | | |
| 40 | 20 | | | | |

Reusable coffee cup

Temperature (°C)

60

50

45

40

38

Time (minutes)

0

10

20

30

40

Check-up

- b) It is claimed that the cup 'keeps 50% of heat for 30 minutes'. Do you agree with this claim? Give evidence for your answer.
- c) Estimate the temperature of the coffee in the disposable cup after 35 minutes.

A new **reusable** coffee cup is tested. The table shows the results.

- Add a new line to your graph which shows the temperature of the coffee in the new reusable cup.
 Label the lines clearly. Add colour and a key like this.
 - ____ Disposable cup
 - ____ Reusable cup
- e) Which cup would you recommend? Give two reasons for your answer.
- f) Copy and complete the claim for the reusable cup: 'Keeps 75% of heat for _ minutes'.
- 6 A Scottish fashion brand sold 1440 items.
 - The pie chart shows the different items sold.

A bag contains 10 discs. Each disc is labelled from

- a) How many bags did the brand sell?
- b) How many scarves did they sell?
- c) How many hats did they sell?

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d) How many purses did they sell?



h)

a prime number

- 1 to 10.Calculate the probability that the first disc picked will be:a) a threeb) an even numberc) six or lessd) at least three
- e) a multiple of three f) a tw

a twelve

g) a factor of 24

BGE S1-S3

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