

# Essential Maths Skills

## for AS/A-level

# Biology

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The listed content is assessed by the awarding bodies AQA, OCR, Pearson Edexcel and WJEC at AS and A-level. **The content listed in bold is only specified to be assessed at A-level.**

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# 1 Arithmetic and numerical computation

## Appropriate units in calculations

Units are very important in biology. Without them numerical values are often meaningless and leaving them out will cost you marks in the exam. You should ensure you can use appropriate units across all calculations and data handling and interconvert different units. You should also be able to derive units where appropriate, for example, in a rate calculation.

A huge range of units is used in biology. You should use the internationally recognised SI units whenever possible (see Table 1.1).

The following table shows how prefixes can be used to give bigger and smaller versions of SI units for length (m), mass (g), volume (m<sup>3</sup>) and surface area (m<sup>2</sup>).

**Table 1.1** SI units

Prefix	Factor	Examples
Deci (d)	$1 \times 10$	dm <sup>3</sup>
Kilo (k)	$1 \times 1000$	kg, km, km <sup>2</sup>
Centi (c)	$\frac{1}{100}$	cm, cm <sup>3</sup>
Mili (m)	$\frac{1}{1000}$	mm, mg, mm <sup>3</sup>
Micro (μ)	$\frac{1}{100\,000}$	μm, μg
Nano (n)	$\frac{1}{1\,000\,000\,000}$	nm, ng

Using the SI unit for length:

$$0.001 \text{ km} = 1 \text{ m} = 100 \text{ cm} = 1000 \text{ mm} = 1\,000\,000 \text{ μm} = 1\,000\,000\,000 \text{ nm}$$

It's important that you select the appropriate unit for each situation. Clearly it would be inappropriate to give the length of an organism in kilometres and, similarly, only the smallest organisms or structures would have their lengths measured in micrometres.

In some cases it is not appropriate to apply a unit to a numerical value, for example, the absorbance measured by a colorimeter. In these cases arbitrary units (sometimes abbreviated to AU) can be given. These units are not standard, cannot be interconverted with any other units and apply only to the results of that particular piece of equipment.

## A Worked examples

- a** What is the length in mm of a bacteria  $50\text{ }\mu\text{m}$  long?

As there are  $1000\text{ }\mu\text{m}$  in  $1\text{ mm}$  you simply divide the value by 1000.

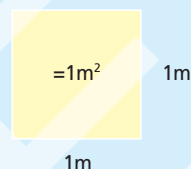
$$\begin{aligned} &= \frac{50}{1000} \\ &= 0.05\text{ mm} \end{aligned}$$

- b** The total surface area of alveoli in a human lung was estimated at  $35\text{ m}^2$ . What is this in  $\text{cm}^2$ ? Show your working.

- Areas are given by lengths squared (e.g.  $\text{m}^2$ ,  $\text{cm}^2$ ,  $\text{mm}^2$ ).
- As  $1\text{ m}$  contains  $100\text{ cm}$ ,  $1\text{ m}^2 = 100\text{ cm} \times 100\text{ cm}$  or  $10\,000\text{ cm}^2$ .
- Similarly  $1\text{ cm}^2 = 10\text{ mm} \times 10\text{ mm} = 100\text{ mm}^2$ .

In this case as  $1\text{ m}^2 = 10\,000\text{ cm}^2$  you must multiply 35 by 10 000.

$$\begin{aligned} &= 35 \times 10\,000 \\ &= 350\,000\text{ cm}^2 \end{aligned}$$



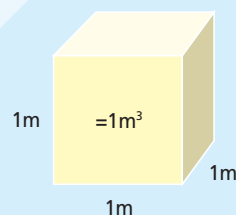
- c** The human body contains  $4700\text{ cm}^3$  of blood. What is this volume in  $\text{m}^3$ ? Show your working.

Volumes are given by  $\text{m}^3$  or  $1\text{ m} \times 1\text{ m} \times 1\text{ m}$ .

- As  $1\text{ m}$  contains  $100\text{ cm}$ ,  $1\text{ m}^3 = 100\text{ cm} \times 100\text{ cm} \times 100\text{ cm}$  or  $1\,000\,000\text{ cm}^3$ .
- Similarly  $1\text{ cm}^3 = 10\text{ mm} \times 10\text{ mm} \times 10\text{ mm} = 1000\text{ mm}^3$ .

In this case as  $1\text{ m}^3 = 1\,000\,000\text{ cm}^3$  you must divide 4700 by 1 000 000.

$$\begin{aligned} &= \frac{4700}{1\,000\,000} \\ &= 0.0047\text{ m}^3 \end{aligned}$$



You can also get the correct answer by  $4700 \times 0.000\,001$ . This is because  $1\text{ cm}^3 = 0.000\,001\text{ m}^3$ .

- d** In an enzyme investigation  $10\text{ g}$  of product was produced in  $30\text{ minutes}$ . What unit would be most appropriate for the rate of this reaction? Calculate the rate of the reaction.

- When measuring mass produced in time, the unit needs to include both mass and time.
- When calculating a rate, the time always goes second in the unit, e.g. mass per time.
- In this case it seems most appropriate to use grams per minute which should be written as  $\text{g min}^{-1}$ .

To calculate the rate of the reaction you need to divide the mass by the time.

$$\begin{aligned} \text{Rate} &= \frac{\text{mass}}{\text{time}} \\ &= \frac{10}{30} \\ &= 0.33 \end{aligned}$$

This gives us a rate of  $0.33\text{ g min}^{-1}$ .

This can be converted into g per second by multiplying by 60. This gives a rate of  $19.8\text{ g s}^{-1}$

## B Guided questions

Copy out the workings and complete the answers on a separate piece of paper.

- 1 What is the mass in grams of a 15 kg soil sample?**

As there are 1000 g in 1 kg you simply multiply the mass in g by 1000.

$$= 15 \times 1000$$

$$= \underline{\hspace{2cm}} \text{ g}$$

- 2 The volume of solution in an investigation was given as 650 mm<sup>3</sup>. What is the volume of this solution in cm<sup>3</sup>?**

There are 1000 mm<sup>3</sup> in 1 cm<sup>3</sup>.

- 3 A student was carrying out an investigation into the rate of change in volume of air in the lungs during a period of exercise. What would be the most appropriate unit to use in this investigation?**

As the student is investigating rate the unit will require a volume component and a time component.

## C Practice questions

- 4** A sample of water from a lake exhibiting signs of eutrophication had a volume of 3.6 dm<sup>3</sup>. What is the volume of this sample in cm<sup>3</sup>?
- 5** In an A-level biological investigation it would be unusual to see volumes given in m<sup>3</sup>. Explain why.
- 6** A measuring cylinder would not be an appropriate piece of apparatus to measure a volume in mm<sup>3</sup>. Explain why.
- 7 a** An ecologist was comparing the flow of energy in a small woodland and a larger area of grassland over several years. When drawing pyramids of energy to compare these two areas what would be the most suitable unit to use?
- b** This same unit would not be suitable for studying energy flow in aquatic ecosystems. Explain why.