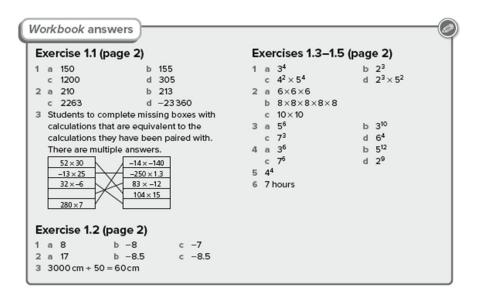
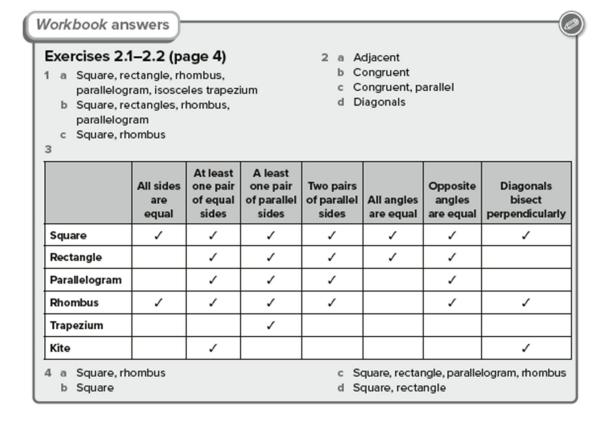
# Cambridge Checkpoint Lower Secondary Mathematics Workbook 8 (2021) Answers

#### Section 1

#### 1 Multiplication and division



## 2 Hierarchy of quadrilaterals



## 3 3 Data collection and sampling methods

#### Workbook answers

## Exercises 3.1-3.4 (page 6)

1

Hair colour	Male	Female	Total
Black	1	1	2
Brown	3	0	3
Blonde	2	3	5
Ginger	0	2	2
Total	6	6	12



- 3 a Categorical. The people were categorised as either male or female.
  - Continuous. Masses can be any number, including decimals.
  - Discrete. Ages are usually just given in years.
  - d Categorical. Hair colours were categorised as black, brown, blonde or ginger.
- 4 a These names will differ as the sample is random.
  - b For example, put the names of the people in a hat and draw out 6 names.

c Student should have added use masses of their sample and of total by 6. d A comparison of their mean as mean 68.5 kg.  5 a They could ask every third powalk into the gym. b They could select students as from each year group. c They could randomly select putheir addresses.	ivided the and the erson to 2 trandom	Never Once Twice Three times More than three times.  a Biased. He has said that most people love using the artificial pitch so this might influence people to say they wished they used it more often. b Answer boxes are subjective. Someone might think that visiting the shop twice a
Exercise 3.5 (page 8)  1 Question should not be biased; should not be subjective, and th boxes should be exhaustive. An could be:  How often do you visit the librar month?	e answer 3 example	week is 'sometimes', whereas someone else might class that as 'often'.  Make sure the sample includes a random sample of students from all year groups.  Duestion should not be biased; answers should not be subjective, and the answer boxes should be exhaustive.

## 4 Parallelograms, trapezia and circles

#### Workbook answers

#### Exercise 4.1 (page 9)

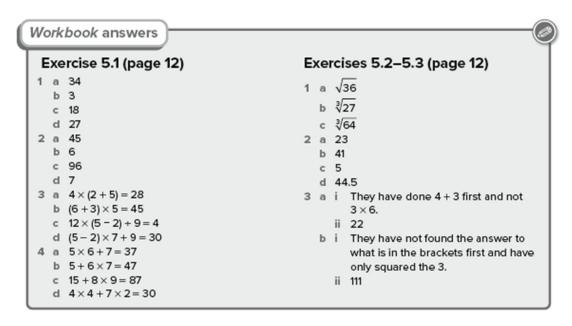
- 1 a 40 cm<sup>2</sup>
  - b 31.5 mm<sup>2</sup>
  - c 75 cm<sup>2</sup>
- 2 a 5.6cm
  - b 2.3 mm
- 3 Parallelogram: 7cm Trapezium: 30cm Triangle: 5.6cm

### Exercise 4.2 (page 10)

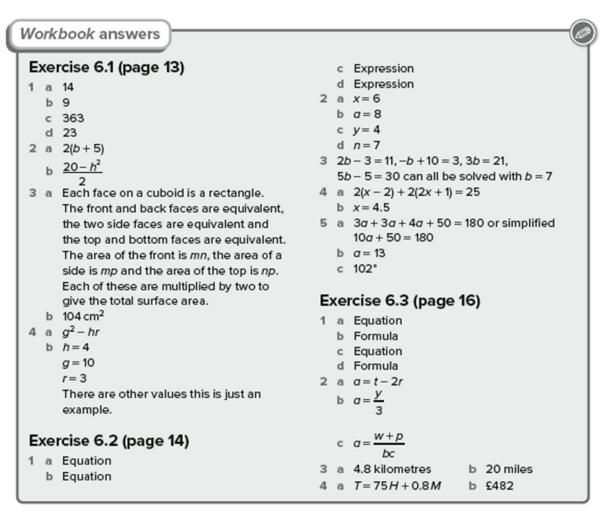
- 1 a 11.31 mm (to 2 d.p.)
  - b 54.04 m (to 2 d.p.)
- 2 a 28.27 cm (to 2 d.p.)
  - b 45.87 mm (to 2 d.p.)
- 3 6 cm
- 4 a \$170.81
  - b 23 cm (to the nearest cm)
- 5 7cm



## 5 Order of operations



## 6 Expressions, formulae and equations



### 7 Recording, organising and representing data

# Workbook answers Exercises 7.1-7.3 (page 17) 1 a Netball b Football c 12 d 28 e 45 i Students may have produced a dual bar chart, like the one shown below. 20 15 10 Football Rugby Netball Hockey Basketball Sports Girls ■ Boys ii Student's own comparisons 2 ■Blue Red Green Yellow Other 3 a Cannot tell because we do not know the total number of students for each pie chart. The proportion of students with brown eyes is higher in group 1 but that does not mean the number of students with brown eyes is higher. b In group 1, the size of the sector is 50 degrees, in group 2 the size of the sector is 165 degrees. Therefore, there is a greater proportion in group 2. c Ben is incorrect because pie charts represent proportions and group 2 has a greater proportion of green-eyed students (i.e. the angle of the slice is greater in group 2 than group 1).

#### Exercise 7.4 (page 19)

```
Exam A
```

1 a

```
 \begin{smallmatrix} 0 & 6 & 8 & 8 \\ 1 & 0 & 2 & 4 & 4 & 6 & 6 & 7 & 8 & 9 \\ 2 & 2 & 3 & 3 & 5 & 7 & 7 & 9 \\ 3 & 0 & & & & & \\ \end{smallmatrix}
```

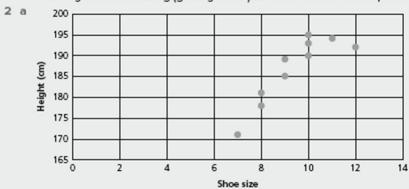
Key 215 means 25 marks

#### Exam B

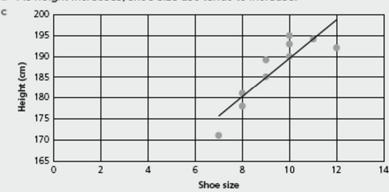
- b Exam A = 18.2, Exam B= 21.7
- c Exam A = 17.5, Exam B = 25
- d Exam A = 8, 14, 16, 23 and 27, Exam B = 26, 27
- e Exam A = 24, Exam B = 20
- f Exam B as the mean and median are both higher than in Exam A.

#### Exercises 7.5-7.6 (page 20)

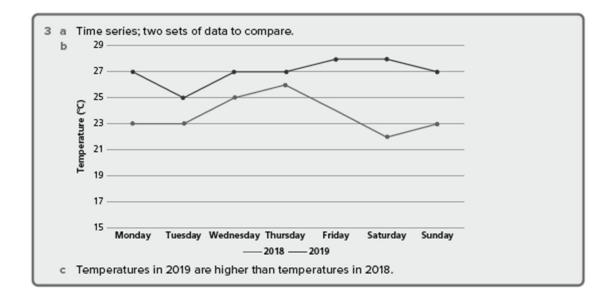
- 1 a No relationship between a person's IQ and their house number.
  - b If the outdoor temperature increases you would expect the sale of barbecues to also increase.
  - c In general the more you train at a sport the better you get. So we would expect to see the finishing time decreasing (getting faster) as the amount of time spent training increases.



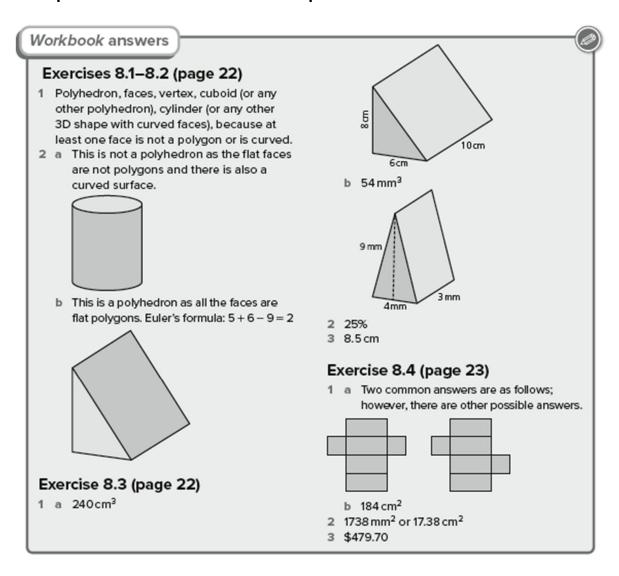
b As height increases, shoe size aso tends to increase.



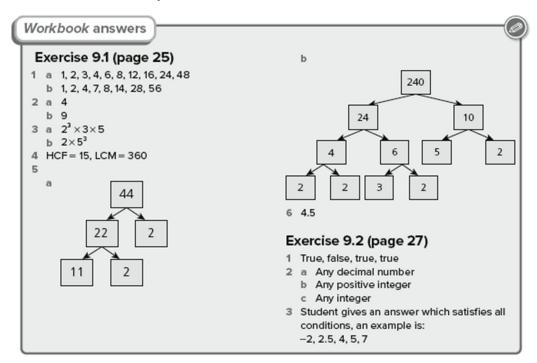
d This answer will vary depending on the line of best fit. For this line of best fit, the height is 182 cm.



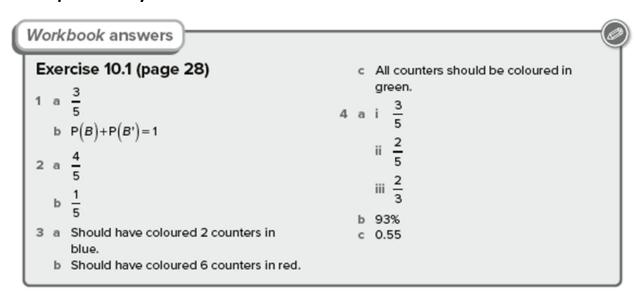
## 8 Properties of three-dimensional shapes



## 9 Factors and multiples



## **10 Complementary events**



### Section 1 - Review



- 1 a Student's explanation, e.g.  $8 \times 4 = 32$ therefore  $80 \times 4 = 320$ 
  - b Student's explanation, e.g.  $(80 \times 4) + (2 \times 4) = 320 + 8 = 328$
  - c Student's explanation, e.g. two negative numbers multiplied produces a positive answer. Therefore,  $-82 \times (-4) = 82 \times 4 = 328$
- 2 a Parallelogram, rhombus, rectangle and square
  - Parallelogram. Student's justification, e.g. all other quadrilaterals in the group have further characteristics which refine their definition.
- 3 a No, it does not, as only 1 out of the 7 chosen is a boy, yet boys make up half of the population of the table.
  - b Student's choice. For example, a random sample that reflects the fact that there are equal numbers of boys and girls in the population.
- 4 a 156 cm<sup>2</sup>
  - b  $A = 12 \text{ cm}^2 B = 24 \text{ cm}^2$
- 5 a 2
  - b 8
- 6 a Candr
  - b 2 and  $\pi$
  - c 31.8 cm

#### 7 a

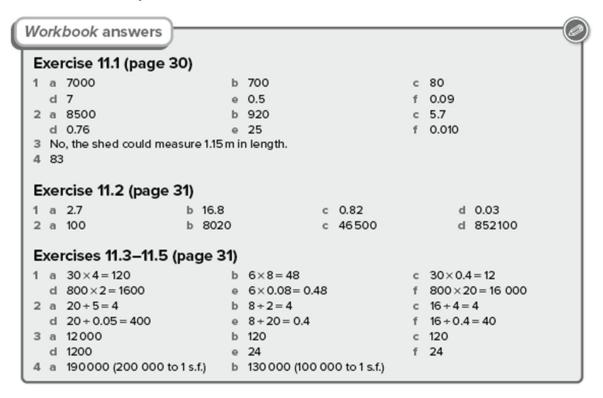
Pizza	Frequency	Percentage	Angle
Margherita	57	19%	68.4°
Pepperoni	21	7%	25.2°
La Reine	105	35%	126°
Fiorentina	81	27%	97.2°
Giardiniera	36	12%	43.2°



- 8 a V = vertices (corners); F = faces; E = edges
  - b V=6; F=5; E=9; 6+5-9=2
- 9 a Factor tree for 48 leading to 2<sup>4</sup> × 3 Factor tree for 70 leading to 2×5×7 HCF=2
  - b LCM =  $2^4 \times 3 \times 5 \times 7 = 1680$
- 10 3/8

#### Section 2

## 11 Decimals and place value



## 12 Comparing and interpreting data

Exercises 12.1–12.2 (page 33)

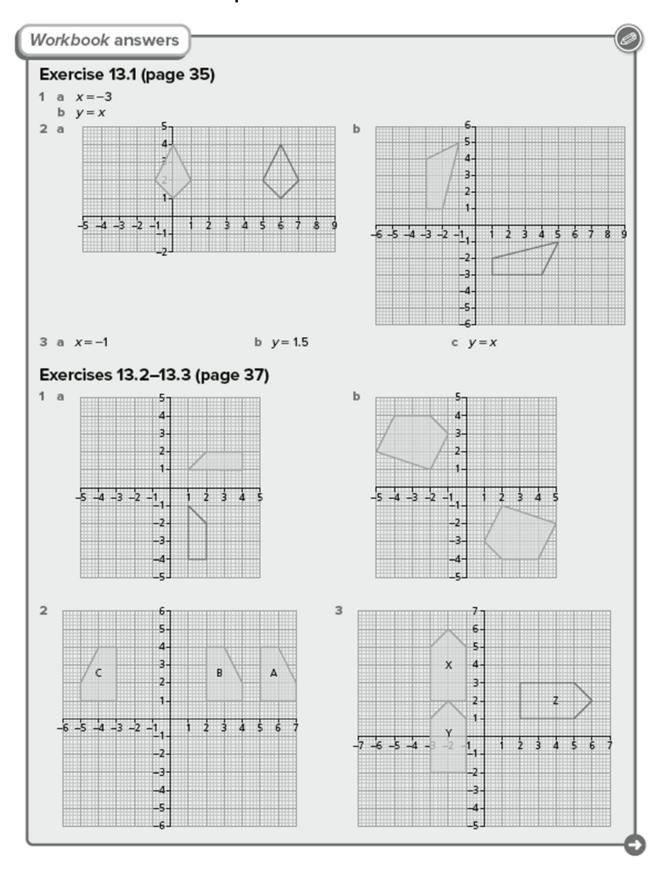
1 a Mean: Season 1 = 1.39, Season 2 = 1.69
 Median: Season 1 = 1, Season 2 = 2
 Mode: Season 1 = 1, Season 2 = 2
 Range: Season 1 = 5, Season 2 = 4

b Season 2 has a higher mean, median and mode so the team scored more goals on average in Season 2. The range is lower in Season 2 as well which suggests the team is more consistent.

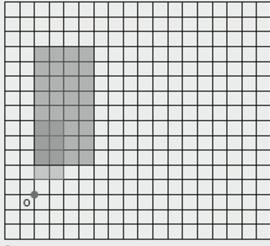
2 Group A is likely to be the group who run 10 km three times a week as the mean, mode and median are all lower and the range is smaller.

3 The summer months are warmer so people will be more likely to eat on the beach.

## 13 Transformation of 2D shapes



## Exercise 13.4 (page 39)



- 3 Centre of enlargement: (1,2)

Scale factor: 2

#### 14 Fractions and decimals

## Workbook answers



## Exercises 14.1-14.2 (page 41)

- 1 a Terminating = 0.25
  - b Recurring = 0.6
    - c Terminating = 0.625
- - b The calculator gives the decimal as 0.1666666667 as it has rounded the last digit that can fit on the screen.
- 3 a  $6 \times 4 = 24$ 
  - b  $14 \times 5 = 70$
  - c 3.2 × 10 3.2 × 0.1 = 31.68

# Exercise 14.3 (page 41) 1 a $3\frac{2}{7}$ b $\frac{12}{5}$ c $2\frac{1}{2}$ d $\frac{28}{5}$ 3 a $17\frac{1}{2}$ 2 a $5\frac{4}{5}$ b $8\frac{2}{7}$ c $3\frac{1}{4}$ d $6\frac{1}{3}$ 3 a $3\frac{11}{20}$ m b $3\frac{1}{8}$ m 4 a $7\frac{13}{20}$

1 a 
$$3\frac{2}{7}$$

2 a 
$$5\frac{4}{5}$$

4 Total of each pair =  $8\frac{1}{12}$ 

$$6\frac{1}{2}$$
 and  $1\frac{7}{12}$ 

$$6\frac{1}{2}$$
 and  $1\frac{7}{12}$   $5\frac{1}{2}$  and  $2\frac{7}{12}$ 

$$3\frac{1}{3}$$
 and  $4\frac{3}{4}$ 

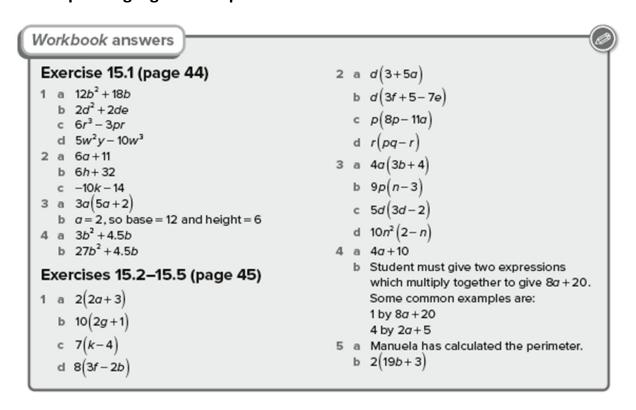
## Exercise 14.4 (page 43)

1 a 
$$16\frac{2}{3}$$

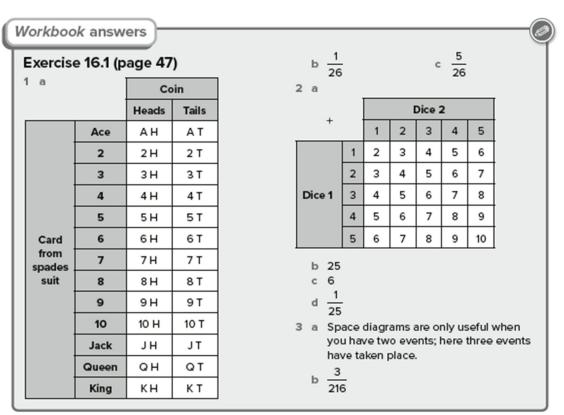
$$b = \frac{5}{2}$$

$$d \frac{b}{a}$$

## 15 Manipulating algebraic expressions



#### **16 Combined events**



#### 17 Constructions, lines and angles

#### Workbook answers

#### Exercises 17.1-17.3 (page 49)

- Students to construct the triangles accurately, showing all construction lines.
- 2 Students to construct the triangles accurately, showing all construction lines
- 3 Cannot be constructed as the angles already sum to over 180 degrees.
- 4 Cannot be constructed as the two shorter sides sum to equal the same length as the longest side.

## Exercises 17.4-17.5 (page 50)

- Students to construct the triangles accurately, showing all construction lines.
- 2 Students to construct the perpendicular bisector of each line, showing all construction lines.
- 3 a-c Students to construct the perpendicular bisector of each line, showing all construction lines.
  - d Yes, the centre of the circle is where all the perpendicular bisectors meet.

#### Exercise 17.6 (page 52)

 Students to bisect each angle, showing all construction lines.

## Exercises 17.7-17.8 (page 52)

- 1  $a = 107^{\circ}$  angles on a straight line sum to 180°.
  - $b = 73^{\circ}$  vertically opposite to 73°.
  - $c = 107^{\circ}$  vertically opposite to a.
- 2  $u = 120^{\circ}$  corresponding to z.
  - $w = 120^{\circ}$  corresponding to z.
  - $y = 60^{\circ}$  angles on a straight line sum to 180°.
  - $z = 120^{\circ}$  vertically opposite 2y.
- 3 a = 20° supplementary angles sum to 180°. b = 80° corresponding to 4a.

#### Exercises 17.9-17.10 (page 53)

- 1  $j = 18^{\circ}$  and  $h = 162^{\circ}$ .
- 2  $t = 113^{\circ}$  as angles on a straight line sum to 180°
  - $u = 33.5^{\circ}$ ,  $s = 33.5^{\circ}$  angles in a triangle sum to 180° and as it is isosceles s and u are equal.
- 3 k = 30° so the four angles are 120°, 90°, 90° and 60°.

## 18 Algebraic expressions and formulae

#### Workbook answers



- 1 a 8n+5
  - $b 3n^2 + 7.5n$
  - c Perimeter = 37 units, Area = 78 units<sup>2</sup>
- $2 \text{ a } 15x^3 9x^2$ 
  - b  $46x^2 24x$
  - Incorrect. x cannot be any negative integer as lengths cannot be negative.
- 3 a N+5
  - b 7

#### Exercise 18.2 (page 56)

- 1 a Option 1: C = 1.2d + 3Option 2: C = d + 3.5
  - b Option 2; it costs \$14 compared to \$15.60 for option 1.
- 2 a £3900
  - b £12500



## 19 Probability experiments

#### Workbook answers

#### Exercise 19.1 (page 58)

- 1 a Depending on results, students will state either biased or unbiased. However, it will be difficult to tell with such a small number of trials.
  - b Students will complete this based on their own experiment.
- 2 a Students to make their spinner using the template.
  - b Students to label each section with the numbers 1–8 in any order.
  - Students will complete this based on their own experiment.

## 20 Equations and inequalities

#### Workbook answers



## Exercise 20.1 (page 60)

- 1 a a = 6c h = -4
- b d = -4
- 2 a g=12
- b n=24
- c b=1
- d t=5
- 3 a m = -7
- b p=7
- c u = -1.5

## Exercise 20.2 (page 61)

- 1 a 15-n=9 so n=6
  - b 2(5+n)=16 so n=3
  - c 4(2+n)=5(n-3) so n=23

## Exercise 20.3 (page 61)

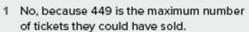
- 1 a a = 3.5
  - b 90

#### 2 Lauren = 27, Georgina = 6, Mia = 14

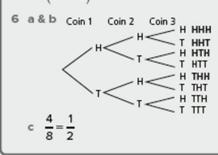
#### Exercises 20.4-20.5 (page 62)

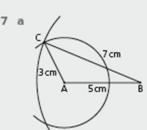
- 1 a a is less than 7
  - b b is greater than or equal to 5
  - c c is not equal to 9
- 2 a 6, 7, 8, 9, 10, 11, 12, 13, 14, 15
  - b 12, 11, 10, 9, 8, 7, 6, 5
  - c -8, -7, -6, -5, -4, -3, -2
- 3 There are other possible answers; the answers below are only examples.
  - $-5 \le c \le 0$
  - -5 ≤ c < 1

#### Section 2 - Review



- 2 a It depends on what is meant by average. Class X's mean and median are greater than Class Y's, but their mode is less.
  - b Class X is more likely to be the one set by ability as the results show class X has a smaller range of results.
- 3 y = 3 and x = -1
- 4 a  $3\frac{1}{5}$  and  $\frac{16}{5}$   $5\frac{1}{5}$  and  $\frac{26}{5}$   $5\frac{4}{5}$  and  $\frac{29}{5}$ 
  - b  $2\frac{2}{5} = \frac{12}{5}$
  - $c = \frac{8}{5} = 1\frac{3}{5}$
- 5 4m(3m+2)







- 8 a  $\frac{13}{2}m + 11$ 
  - b i m=2 ii 6kg, 8kg and 10kg
- 9 a Four flips of a coin is not enough times to determine whether it is biased.
  - b Yes, by flipping the coin a large number of times.

10 
$$2(x+4)=4x-2$$
  
  $x=5$ 

#### Section 3

## 21 Describing sequences

#### Workbook answers

## Exercise 21.1 (page 63)

- 1 a  $3\frac{1}{4}$ ,  $3\frac{1}{2}$ ,  $3\frac{3}{4}$ b 6, 3, 1.5

  - $c -4\frac{1}{3}, 5, -4\frac{1}{3}$
- 2 a 6, 10, 14, 18, 22
  - b 2, 5, 8, 11, 14
  - c -4, -2, 0, 2, 4
- 3 a 16, 32; 10th term = 20
  - b  $\frac{3}{5}$ ,  $\frac{2}{5}$ ; 10th term =  $-\frac{2}{5}$
- c 80, -160; 10th term = -2560
- 4 a 17
  - b Number of squares
    - = pattern number  $\times$  2+1

  - d No, as all patterns have an odd number of squares.

## Exercise 21.2 (page 64)

- 1 a nth term = 3n+150th term = 151
  - b nth term = 4n-1050th term = 190
  - c nth term = 2.5n 1.550 th term = 123.5
- 2 Both sequences have the number 26 in them, when n = 5.
- 3 a Students should draw the next two cuboids. The second cuboid is 4 cubes high and 2 cubes wide. The third cuboid is 5 cubes high and 3 cubes wide.
  - b No, you need 255 cubes to make cuboid 15. It will be 17 cubes high and 15 cubes wide.  $17 \times 15 = 255$ .

## 22 Percentage increases and decreases

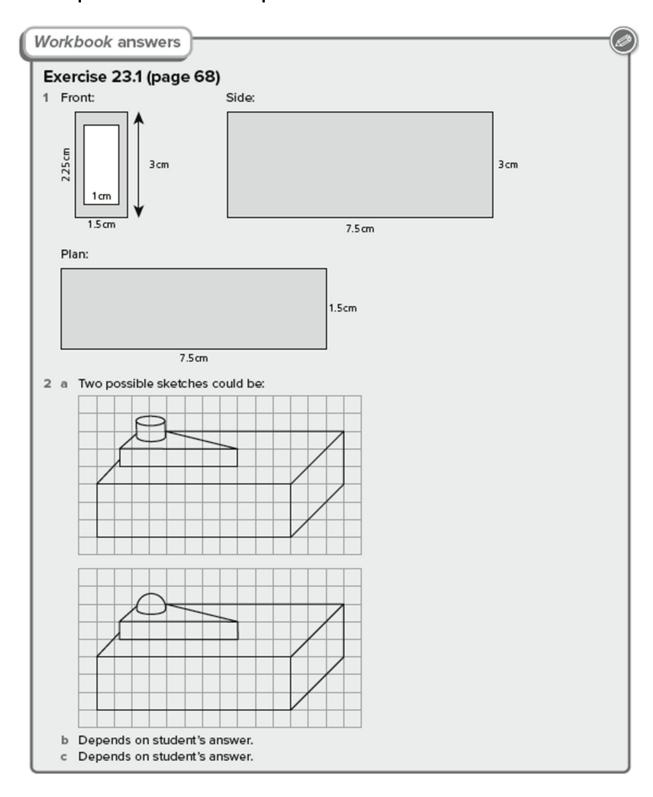
#### Workbook answers



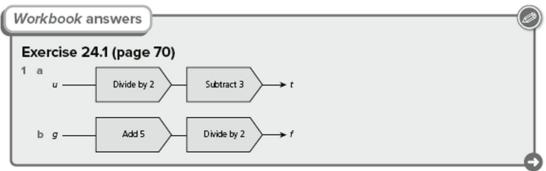
- 1 a 180
  - b 896
  - c 748.8
  - d 39.2

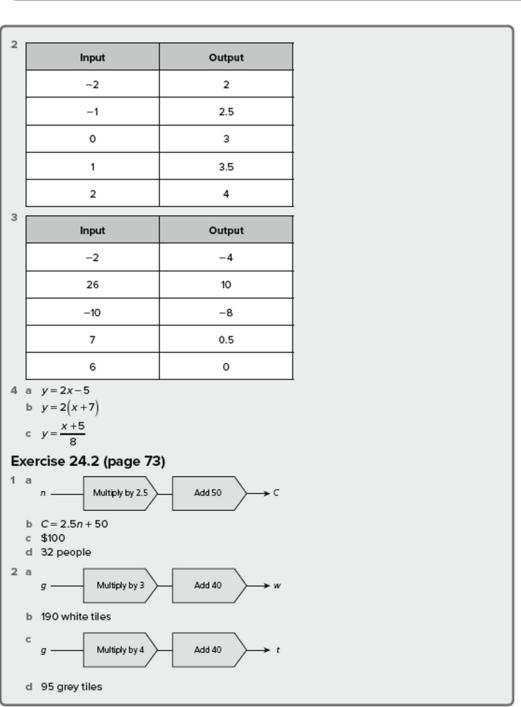
- 2 a Shop A; selling for \$405 compared to \$434
  - b \$135
- 3 \$158
- 4 11.2 m below sea level
- 5 98.4% increase

## 23 2D representations of 3D shapes



#### 24 Functions

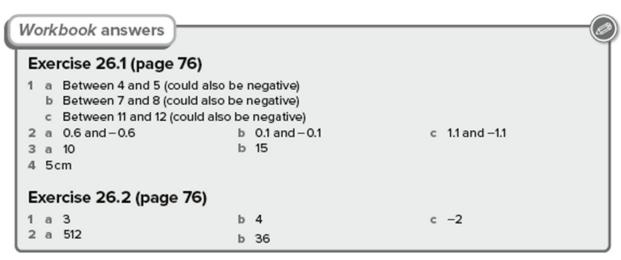




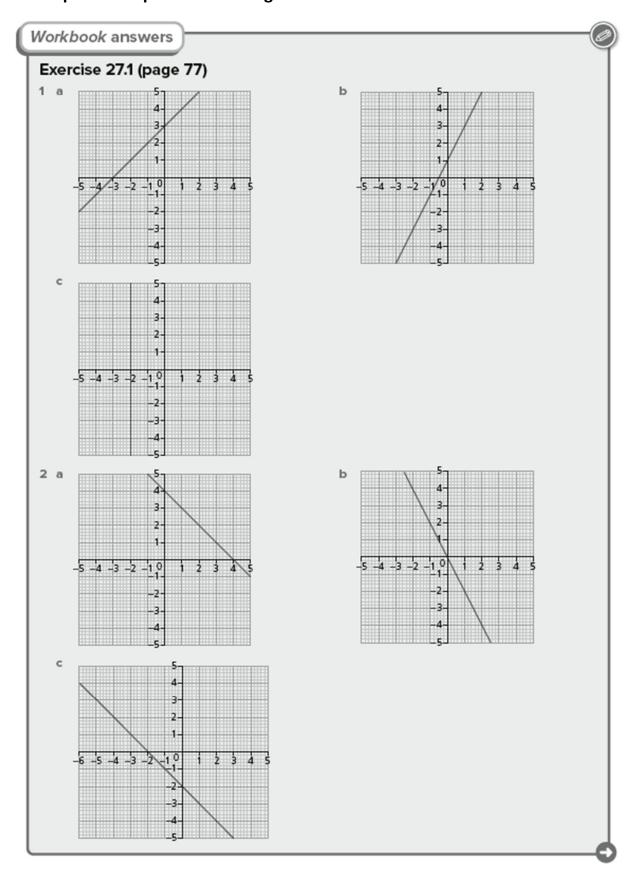
## 25 Geometry and translations

## Workbook answers Exercise 25.1 (page 73) 1 a Midpoint = (5, 7) b Midpoint = (-4.5, 5) 6-5--10-9-8-7-6-5-4-3-2-10 2 3 4 5 6 7 8 9 10× 2 (3, 9) 3 P = (-10, -1), Q = (-10, 9), R = (6, 9) Exercise 25.2 (page 74) G to F reverses the direction so instead of going 1 2 2 2 to the right and 5 down, you get back to F. You have to go 2 to the left and 5 up. 4 J'= (0, 2) K' = (-2, -1)L' = (2, -4)

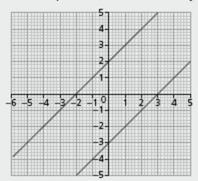
## 26 Squares, square roots, cubes and cube roots



## 27 Graphs and equations of straight lines



- 3 Two straight lines will only cross at a maximum of 1 point. If they cross more than once, at least one of the lines must be curved.
- 4 Students plot the lines to show they are parallel. Parallel lines will never meet.



#### Exercise 27.2 (page 79)

- 1 y = 3x
- 2 y = 2x + 1
- 3 a y = any number
  - b Any line in the form y = mx + c
  - c x = any number

#### Exercise 27.3 (page 80)

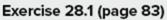
- 1 a  $y = 2x \pm a$
- b y = ax + 1 (a can be any number)
  - C: y = 2x
- D: x = 4

- 2 A: y = -x + 2E: y = x + 1
- B: y = 3x + 2F: y = x
- G: y = -2

- 3 a C = 10d + 45
- b 3 days

## 28 Distances and bearings

#### Workbook answers



- 1 a 192 km
  - b 937.5 miles
  - c 55 miles
- 2 32 km or 20 miles

## Exercise 28.2 (page 83)

Students' bearings may differ from these by  $\pm 2^{\circ}$ .

1 a 120°

- b 045°
- c 225°
- 2 a 032° b 115°
  - c 160°
  - d 295°
- 3 a 280km
- b She has measured the bearing anticlockwise rather than clockwise.
  - c Bearing 130°; Distance 240 km

#### 29 Ratio

#### Workbook answers

## Exercises 29.1-29.2 (page 86)

- 1 a Yes,  $1 \times 4 = 4$ ,  $5 \times 4 = 20$ 
  - b No,  $7 \times 2 = 14$  but  $8 \times 2 \neq 15$
  - c Yes,  $3 \times 9 = 27$ ,  $5 \times 9 = 45$
- 2 a 3:5
- b 5:11
- 3 a 5:2
- b 3:10
- 4 First drink is more concentrated. An equivalent fraction to 1:10 is 2:20 compared to the second drink which is 2:25. More water for 2 parts of cordial in the second drink.

## Exercise 29.3-29.4 (page 86)

- 1 a 120 and 200
  - b 96 and 224

- 2 a  $\frac{2}{7}$ 
  - b 20
- 3 a 108°
  - b Angles in a quadrilateral sum to 360°.
- 4 a 2:1
  - b 18:5

## Exercise 29.5 (page 88)

- 1 \$6.08
- 2 112.5 miles
- 3 5 hours

## 30 Reading and interpreting graphs

#### Workbook answers

#### Exercise 30.1 (page 89)

- 1 a Horse A: it reaches 3 miles in less time than horse B.
  - b 40 seconds
  - 4 minutes and 40 seconds, the line became steeper.
- 2 a 60 m
  - b 6 seconds
  - True: ball A is in the air for 6 seconds, ball B for 7 seconds.
    - ii True: ball B was fired 2 seconds after
    - iii False: ball B went 20m higher than ball A.

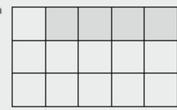
## Exercise 30.2 (page 91)

- 1 a Sharifa gets into the bath.
  - b 9 minutes: water level suddenly goes down at 18 minutes.
- 2 a Oven A reaches 100°C after 5 minutes compared to oven B which reaches 100°C after about 12 minutes.
  - b 18-19°C. They are at room temperature.
  - с В
  - d 18 minutes: the lines cross at this point.

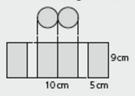


#### Section 3 - Review





- b Add 2
- c 2n+3
- d 43
- 2 a -21°C
  - b −27°C
- 3 Scale drawing as follows:



- 4 a  $y = \frac{x+2}{5}$ 
  - b  $y = \frac{x}{4} 3$



5 To prove ABCD is a parallelogram, midpoints of diagonals cross at the same point.

Midpoint AC = 
$$\left(4, 2\frac{1}{2}\right)$$

Midpoint BD = 
$$\left(4, 2\frac{1}{2}\right)$$

Therefore, a parallelogram.

- 6 Student's method showing √0.49 = 0.7
- 7 (9, -1) and (-12, -8)
- 8 a Student's drawing of A and B. (Accept ±1° and ±1mm error).
  - b 238° (Accept ±2°)
- 9 Student's use of three colours. Number of squares coloured 8:16:40
- 10 a Graph 1 is tariff B. Graph 2 is tariff A. Student's explanation. y-intercepts are 40 and 20, respectively.
  - b Tariff B because for a value of 60, the graph for tariff B is below that for tariff A, implying it is cheaper.
  - Either, because that is approximately where the graphs intersect.